

# SHEKHAWATI INSTITUTE OF ENGINEERING & TECHNOLOGY

SIKAR , RAJASTHAN



1<sup>st</sup> -MID TERM EXAMINATION 2018 (6<sup>th</sup> Semester -ME)

Subject Code & Name: 6ME1A (MD-2.)

MM: 20

Time: 1 :30H

## Student Instruction

1. Use pencil for diagrams.
2. Answer should mark proper S No.
3. **Attempt any five question**  
all

1A helical spring is made from a wire of 6mm dia. And has outside Diameter of 75mm. if the permissible shear stress is 350Mpa and modulus of rigidity  $84\text{KN/mm}^2$ , find the axial load which the spring can carry and the deflection per active coil?

2 Explain the different type of anti friction bearing ?

3 Derive the expression for bending strength of the gear?

4 derive the expression for helical spring under axial compressive load and friction coefficient for journal bearing?

5 A single row angular contact ball bearing number 310 is used for an axial load . the bearing is to carry a radial load of 2500N and thrust load of 1500N .assuming light shock load ,determine the rating life of the bearing?



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Model Answer Paper

Q.1

A helical spring is made from a wire of 6mm diameter and has outside diameter of 76mm. If the permissible shear stress is 350MPa and modulus of rigidity 84 kN/mm<sup>2</sup>, find the axial load which can carry and the deflection per active turn.

Sol<sup>n</sup>

Given

$$d = 6 \text{ mm}, \quad D_o = 76 \text{ mm}, \quad \tau = 350 \text{ MPa}$$

$$\tau = 350 \text{ N/mm}^2, \quad C = 84 \text{ kN/mm}^2 = 84 \times 10^3 \text{ N/mm}^2$$

We know that mean diameter of the spring

$$D = D_o - d = 76 - 6 = 70 \text{ mm}$$

$$\therefore \text{Spring index, } C = \frac{D}{d} = \frac{70}{6} = 11.67$$

Let,  $W$  = Axial load.

$\delta/m$  = Deflection per active turn.

i) Neglecting the effect of curvature.

We know that shear stress,

$$k_s = 1 + \frac{1}{2C} = 1 + \frac{1}{2 \times 11.67} = 1.043$$

maximum shear stress induced in the wire. (2)

$$350 = k_s \times \frac{8WD}{\pi d^3} = 1.043 \times \frac{8W \times 70}{\pi d^3} = 0.848W$$

$$W = 350 / 0.848 = 412.7 \text{ N} \quad \underline{\underline{\text{Ans}}}$$

We know that the deflection of the spring.

$$\delta = \frac{8 \cdot W \cdot D^3 \cdot n}{w \cdot d^4}$$

∴ Deflection per active turn.

$$\frac{\delta}{n} = \frac{8 \cdot W \cdot D^3}{w \cdot d^4} = \frac{8 \times 412.7 (69)^3}{84 \times 10^3 \times 6^4}$$

$$\boxed{\frac{\delta}{n} = 9.96 \text{ mm}} \quad \underline{\text{Ans}}$$

2) Considering the effect of curvature.

We know that Wahl's stress factor.

$$k = \frac{4C-1}{4C-4} + \frac{0.615}{C}$$

$$k = \frac{4 \times 11.5 - 1}{4 \times 11.5 - 4} + \frac{0.615}{11.5}$$

$$\boxed{k = 1.123}$$

maximum shear stress induced in the wire (2)

$$350 = k \times \frac{8 \cdot W \cdot C}{\pi d^3} = 1.123 \times \frac{8 \times W \times 11.5}{\pi \times 6^3} = 0.913 W$$

$$W = 350 / 0.913$$

$$\boxed{W = 383.4 \text{ N}} \quad \underline{\text{Ans}}$$

Deflection of the spring

$$\delta = \frac{8 \cdot W \cdot D^3 \cdot n}{w \cdot d^4}$$

∴ Deflection per active turn.

$$\frac{\delta}{n} = \frac{8 \cdot W \cdot D^3}{w \cdot d^4} = \frac{8 \times 383.4 (69)^3}{84 \times 10^3 \times 6^4} = 9.96 \text{ mm} \quad \underline{\underline{\text{Ans}}}$$

Q.2 Explain the different type of anti friction bearing?

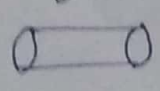
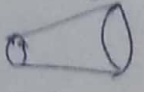

Ans:- There are two types of anti friction bearing.

- a) Ball Bearing.
- b) Roller Bearing.

### Types of Ball Bearing:

<p>1) <u>Deep Groove B.B</u></p> <ol style="list-style-type: none"> <li>i) <math>f_r/f_a &gt; 1</math></li> <li>ii) construction simple</li> <li>iii) Cost (min)</li> <li>iv) mostly used.</li> </ol>	<p>2) <u>Angular Contact Ball Bearing</u></p> <ol style="list-style-type: none"> <li>i) <math>f_o/f_a &lt; 1</math></li> <li>ii) construction is difficult</li> <li>iii) Cost high.</li> <li>iv) Free land bearing is required</li> </ol>	<p>3) <u>Self Alignment Ball Bearing</u></p> <ol style="list-style-type: none"> <li>i) permit mis alignment b/w shaft and bearing house</li> <li>ii) <math>f_a</math> and <math>f_o</math> both angular be used</li> </ol>	<p>4) <u>Thrust Ball Bearing</u></p> <ol style="list-style-type: none"> <li>i) <math>f_r</math> (only)</li> <li>ii) only for vertical shaft</li> <li>iii) <math>f_r = 0</math></li> </ol>
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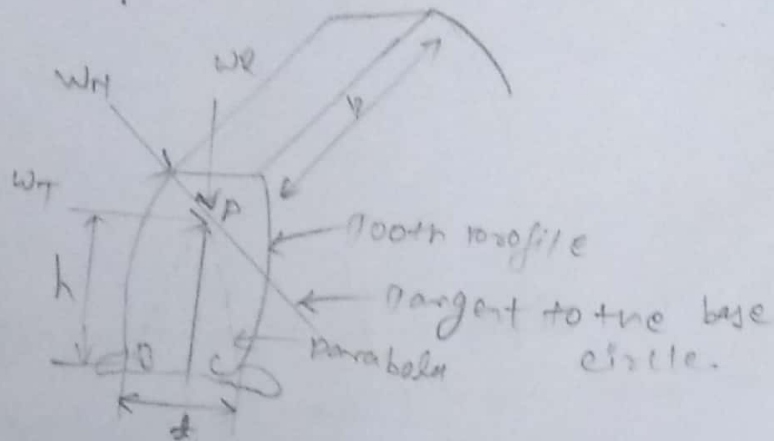
### Types of Roller Bearing:

<p>1) <u>Spherical Roller Bearing</u></p> <ol style="list-style-type: none"> <li>i) permit mis alignment</li> <li>ii) Full Row of Roller Bearing</li> <li>iii) <math>f_r</math> and <math>f_a</math> Both.</li> </ol>	<p>2) <u>Critical Roller Bearing</u></p> <ol style="list-style-type: none"> <li>i) <math>f_r</math> </li> <li>ii) <math>f_a = 0</math></li> <li>iii) Preferred for horizontal shaft</li> <li>iv) maximum Radial load capacity</li> </ol>	<p>3) <u>Taper Roller Bearing</u></p> <ol style="list-style-type: none"> <li>i) </li> <li>ii) <math>f_r/f_a &gt; 1</math></li> <li>iii) maximum load bearing.</li> <li>iv) construction is difficult.</li> </ol>	<p>4) <u>Needle Roller Bearing</u></p> <ol style="list-style-type: none"> <li>i) </li> <li>ii) Needle R.B are used when Radial space Constrained.</li> <li>iii) used at pressure trans.</li> </ol>
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Q.3

Derive the expression for bending strength of the gear?

Ans:



$$\sigma_w = m \cdot y / I$$

$m$  = maximum bending moment.

$W_T$  = tangential load acting.

$h$  = length of the tooth.

$y$  = half the thickness.

$I$  = moment of inertia.

$b$  = width of the gear.

$$\sigma_w = \frac{(W_T \times h) \cdot t/2}{bt^3/12} = \frac{(W_T \times h) \times 6}{bt^2}$$

$$W_T = \sigma_w \times b \times t^2 / 6h$$

Let  $t = n \times P_c$  and  $h = k \times P_c$   $n$  and  $k$  are constant

$$W_T = \sigma_w \times b \times \frac{n^2 \cdot P_c^2}{6k \cdot P_c}$$

$$W_T = \sigma_w \times b \times P_c \times \frac{n^2}{6k}$$

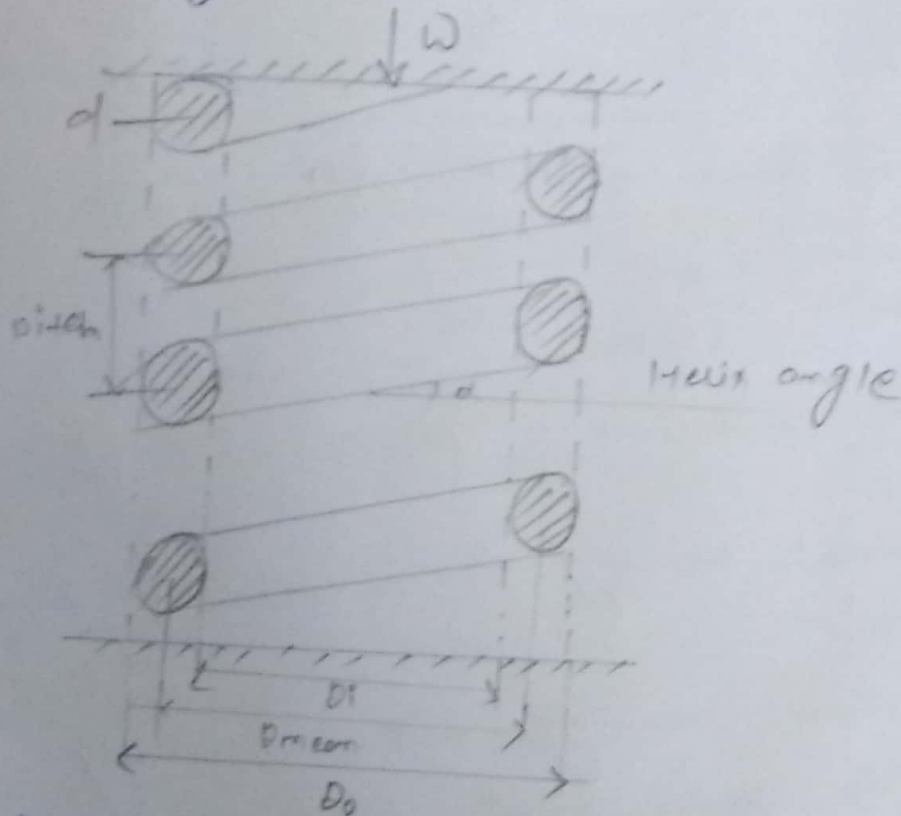
$$W_T = \sigma_w \cdot b \cdot P_c$$

$$y = \sigma_w \cdot b \cdot \pi m \cdot y$$

$$\therefore y = \frac{n^2}{6k} = \frac{t^2}{(P_c)^2} \times \frac{P_c}{6h} = \frac{t^2}{6 \cdot h \cdot P_c}$$

Q.4 Derive the expression for helical spring under axial compressive load and friction coefficient for journal bearing.?

Ans → Helical spring under axial compressive load.



$D$  = mean dia.

$$D = D_i + d = D_o - d$$

$C$  = Spring index.

$$\boxed{C = \frac{D}{d}} \quad \boxed{4 \leq C \leq 12}$$

$n$  = no. of active coils.

$$Z_{dia} = \frac{P}{A} = \frac{W}{\pi d^2}$$

$$\tau_{dir} = \frac{4W}{\pi d^2}$$

$$\tau = \frac{T}{J}$$

$$\tau_{max} = \frac{TR}{J} = \frac{\frac{WD \times d/2}{2} \times d/2}{\frac{\pi d^4}{32}}$$

$$\tau_{max} = \frac{8WD}{\pi d^3}$$

$$\tau_{max} = \tau_{shear} + \tau_{twisting}$$

$$\tau_{max} = \frac{4W}{\pi d^2} + \frac{8WD}{\pi d^3}$$

Inner point on maximum load.

Outer point minimum load.

$$W_{max} = \frac{\pi d^3}{8W} \times \tau_{per}$$

friction coefficient of journal bearing.

- Journal bearing is a sliding contact radial load.
- Journal bearing with generally operating with hydrodynamic lubrication.

$$c_1 = R_1 - R_0 = \text{Radial clearance.}$$

$$C = D_1 - D_0 = \text{Diametrical clearance.}$$

$l =$  length of bearing

$$C = 2c_1$$

$$2R_1 - 2R_0 = C, \quad 2(R_1 - R_0) = C$$

$$2c_1 = C$$

Q.5 A single row angular contact ball bearing number 310 is used for an axial load. The bearing is to carry a radial load of 2500 N and thrust load of 1500 N. Assuming light shock and determine the rating life of the bearing?



Given:

$$W_R = 2500 \text{ N}; \quad W_A = 1500 \text{ N}$$

$$W_A/W_R = 1500/2500 = 0.6$$

$$x = 1 \quad \text{and} \quad y = 0$$

The rating factor (V) for the material of the bearing.

$$W = x \cdot V \cdot W_R + y \cdot W_A = 1 \times 1 \times 2500 + 0 \times 1500 = 2500 \text{ N}$$

$$\boxed{W = 2500 \text{ N}}$$

We find the factor for light shock.

$$\boxed{W = 2500 \times 1.5 = 3750 \text{ N}}$$

For a single row angular contact ball bearing number 310.

$$\boxed{C = 53 \text{ kN} = 53000 \text{ N}}$$

We know that rating life of the bearing in revolution

$$L = \left(\frac{C}{W}\right)^k \times 10^6 = \left(\frac{53000}{3750}\right)^3 \times 10^6$$

$$\boxed{L = 2823 \times 10^6 \text{ rev}}$$

Ans

$$\boxed{\therefore k = 3}$$